

**JOSAI
MATHEMATICAL
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13

2021

**Representations of
Discrete Groups
and
Geometric Topology on
Manifolds**

JOSAI UNIVERSITY

Edited by
Haruko NISHI
Yoshinobu KAMISHIMA
Masatoshi IIDA



JOSAI UNIVERSITY
GRADUATE SCHOOL OF SCIENCE

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Keyakidai 1-1, Sakado
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Haruko Nishi, Editor in Chief

Contents

<i>Preface</i>	iv
GENKI SHIBUKAWA, <i>A revisit to periodic continuants</i>	3
MASAYUKI YAMASAKI, <i>Rotation numbers of regular closed curves on oriented aspherical surfaces</i>	19
HISASHI KASUYA, <i>Introduction to variations of Hodge structure over Sasakian manifolds</i>	31
YOSHINOBU KAMISHIMA, <i>Construction of contractible complete quaternionic almost Hermitian manifolds with compact isometry group</i>	53
SHINJI OHNO AND TAKASHI SAKAI, <i>Area-minimizing cones over minimal embeddings of R-spaces</i>	69
SHIGEYASU KAMIYA, <i>Complex hyperbolic triangle groups of type $(n, n, \infty; k)$</i>	93
MARTIN A. GUEST AND NAN-KUO HO, <i>Polytopes, supersymmetry, and integrable systems</i>	109
AKIFUMI OCHIAI, <i>Special Lagrangian submanifolds and Lagrangian mean curvature flows with generalized perpendicular symmetries</i>	137
FRANÇOIS FILLASTRE AND ANDREA SEPPI, <i>A remark on one-harmonic maps from a Hadamard surface of pinched negative curvature to the hyperbolic plane</i>	163
SUMIO YAMADA, <i>Variations of complex and hyperbolic structures on Riemann surfaces – a comparative viewpoint –</i>	173

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SUMIO YAMADA, <i>Variations of complex and hyperbolic structures on Riemann surfaces – a comparative viewpoint –</i>	173